



# EFM-EDHEC Symposium

## Risk and Asset Management

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### UK Mutual Fund Performance: Skill or Luck ?

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# Introduction

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- Study examines the abnormal (risk adjusted) performance of the UK equity unit trust industry between April 1975 – Dec 2002.
- Evaluates whether funds possess 'genuine' stock picking ability, controlling for sampling variability in performance (chance).
- Bootstrap simulations generate a distribution under the null at each point in the cross-section distribution of performance.
- Kosowski et al (2006), JoF.



# Data

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- Sample period: Monthly returns April 1975 – December 2002
- Data set of 1,620 funds (Unit Trusts and OEICs)
- 842 'Independent' funds (excl 2<sup>nd</sup> units and trackers)
- Investment Objectives classified by IMA:
  - Equity Income (162)
  - General Equity (553)
  - Smaller Companies (127)
- 626 surviving funds, 216 nonsurviving funds
- 662 onshore, 180 offshore



# Performance Measurement: Model Selection

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## Unconditional Three-Factor Model

$$R_{i,t} = \alpha_i + \beta_1(R_{m,t}) + \beta_2(\text{SMB})_t + \beta_3(\text{HML})_t + U_t$$



# Model Selection

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## Conditional Beta Model

$$R_{i,t+1} = \alpha_i + \beta_{it} (R_{m,t+1}), \quad \beta_{it} = b_{i,0} + B'_i(z_t)$$

$$R_{i,t+1} = \alpha_i + b_{i,0} (R_{m,t+1}) + B'_i(z_t \cdot R_{m,t+1}) + U_{t+1}$$

Z (in deviations): market dividend yield, short term rate, gilt:equity yield ratio, term spread, credit spread

Model Selected based on SIC

$$R_{i,t+1} = \alpha_i + \beta_1 (Rm)_{t+1} + \beta_2 (SMB)_{t+1} + \beta_3 (HML)_{t+1} + \beta_4 [(R_{m,t+1}) * (z_t)] + U_{t+1}$$

where  $z_t$  = dividend yield

# Model Selection

## Conditional Alpha-Beta Models

$$r_{j,t+1} = \alpha_j + \beta_j'(F_{t+1}) + U_{j,t+1} \quad R_{i,t+1} = \sum_{j=1}^N W_{j,t+1} \cdot r_{j,t+1} \quad W_{j,t+1} = W_{j,0} + W_j'(z_t)$$

$$\begin{aligned} R_{i,t+1} &= \sum_{j=1}^N [(W_{j,0} + W_j'z_t) \cdot (\alpha_j + \beta_j'F_{t+1} + U_{j,t+1})] \\ &= \sum_{j=1}^N W_{j,0} \cdot \alpha_j + \sum_{j=1}^N W_j' \alpha_j z_t + \sum_{j=1}^N W_{j,0} B_j' F_{t+1} + \sum_{j=1}^N W_j' z_t B_j' F_{t+1} \\ &\quad + \left[ \sum_{j=1}^N W_{j,0} \cdot U_{j,t+1} + \sum_{j=1}^N W_j' z_t U_{j,t+1} \right] \end{aligned}$$

$$R_{i,t+1} = [\alpha_{i,0} + A_i'(z_t)] + b_{i,0}'(F_{t+1}) + B_i'(z_t, F_{t+1}) + U_{i,t+1}$$

Model Selected (based on SIC):

$$R_{i,t+1} = \alpha_i + A_i(z_t) + \beta_1(R_{m,t+1}) + \beta_2(\text{SMB})_{t+1} + \beta_3(\text{HML})_{t+1} + \delta_1(R_{m,t+1} \cdot z_t) + \delta_2(\text{SMB}_{t+1} \cdot z_t) + \delta_3(\text{HML}_{t+1} \cdot z_t) + U_{i,t+1}$$

where  $z_t$  = dividend yield



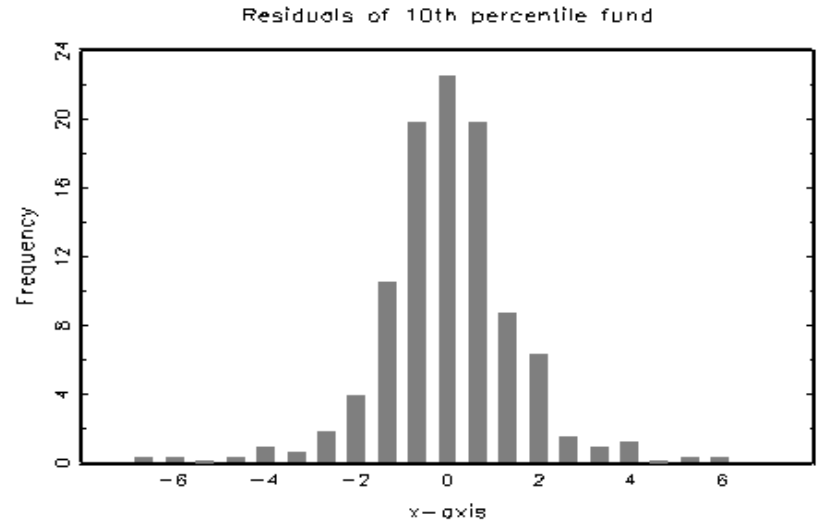
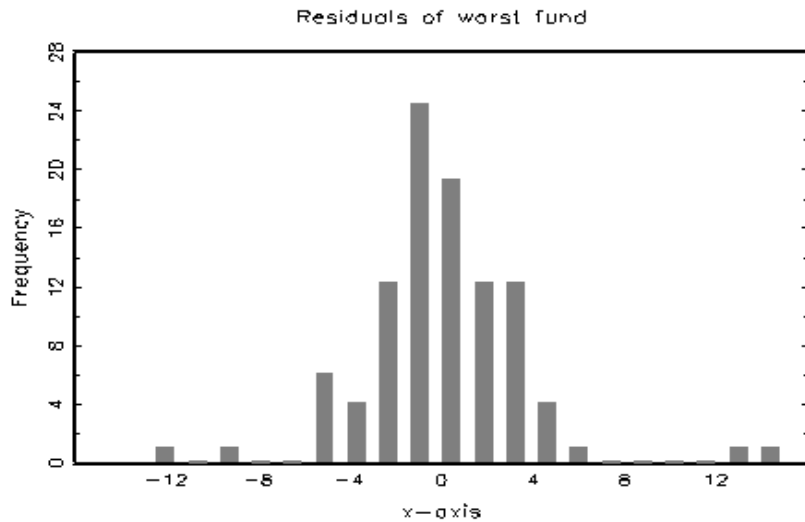
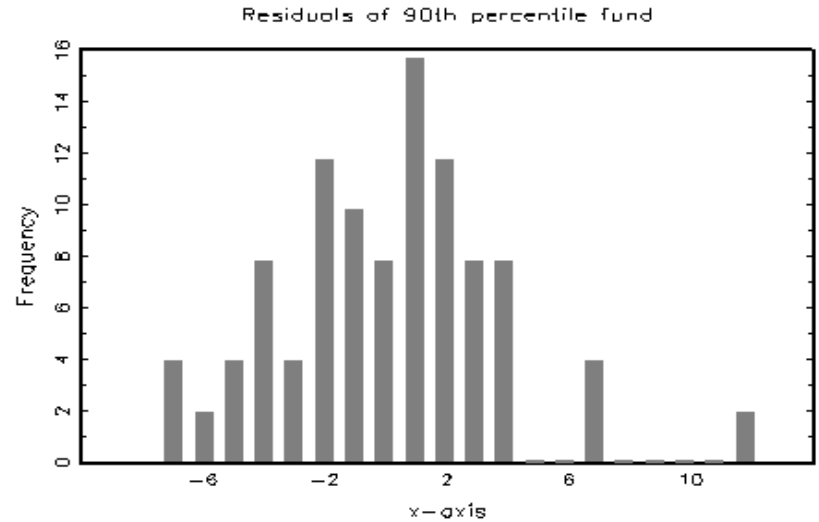
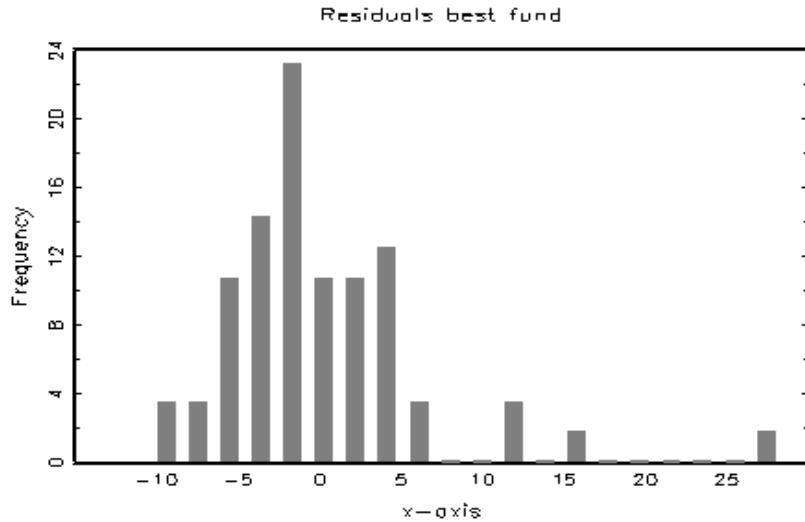
# Model Inferences

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- A total of 54 models were estimated
- Alpha measures abnormal (risk adjusted) performance
- Standard inference tests require normality for validity
- Given large number of funds some will appear to do well/badly by chance – need to establish the role of luck
- Investors are more interested in funds in the tails of the performance distribution

# Problem: non-normal 'luck'

## Residuals (Fama-French 3Factor)





# Methodology

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- Why Bootstrap?
  - Bootstrap is nonparametric: makes no assumption about 'true' shape of the distribution
  - Procedure establishes the nonparametric distribution at *each* point/percentile of performance.



# Methodology

- Cross-sectional bootstrap procedure:

- Estimate model, save coefficients and residuals

$$R_{i,t+1} = \hat{\alpha}_i + \hat{\beta}_1 (R_{m,t+1}) + \hat{\beta}_2 (\text{SMB})_{t+1} + \hat{\beta}_3 (\text{HML})_{t+1} + \hat{\varepsilon}_{i,t+1}$$

- Bootstrap simulation (with replacement) for fund  $i$  under the null hypothesis of zero abnormal performance, i.e.  $\alpha_i = 0$ .
- Construct  $\tilde{R}_{i,t}$  and estimate  $\tilde{\alpha}_i$
- Perform for  $B = 1, 2, \dots, 1000$  simulations on *each* fund  $i = 1, 2, \dots, N$ ,  $N = 675$ .
- Within each simulation across funds, sort  $\tilde{\alpha}_i$  from high to low
- This provides an estimate of the distribution of abnormal performance (under the null of no abnormal performance) at *each* point in the performance distribution, i.e. an estimate of random sampling variation.
- Here, luck distributions capture the valuable information (standard deviation) in *all* funds – not just fund by fund.
- Each distribution of  $\tilde{\alpha}_i$  is a function of  $\text{var}(\hat{\varepsilon}_{i,t}) \forall i = 1, 2, \dots, N$

# 'Luck' Distributions, bootstrap alphas and p-values

$$\widetilde{\alpha}_{1,1}^{b,1}, \widetilde{\alpha}_{1,1}^{b,2}, \dots, \widetilde{\alpha}_{1,1}^{b,B}$$

$$\widetilde{\alpha}_{2,1}^{b,1}, \widetilde{\alpha}_{2,1}^{b,2}, \dots, \widetilde{\alpha}_{2,1}^{b,B}$$

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$$\widetilde{\alpha}_{N,1}^{b,1}, \widetilde{\alpha}_{N,1}^{b,2}, \dots, \widetilde{\alpha}_{N,1}^{b,B}$$

$$f(\alpha_{\max}) : \widetilde{\alpha}_{H,1}^{b,1}, \widetilde{\alpha}_{H,1}^{b,2}, \dots, \widetilde{\alpha}_{H,1}^{b,B}$$

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$$f(\alpha_{\min}) : \widetilde{\alpha}_{L,1}^{b,1}, \widetilde{\alpha}_{L,1}^{b,2}, \dots, \widetilde{\alpha}_{L,1}^{b,B}$$



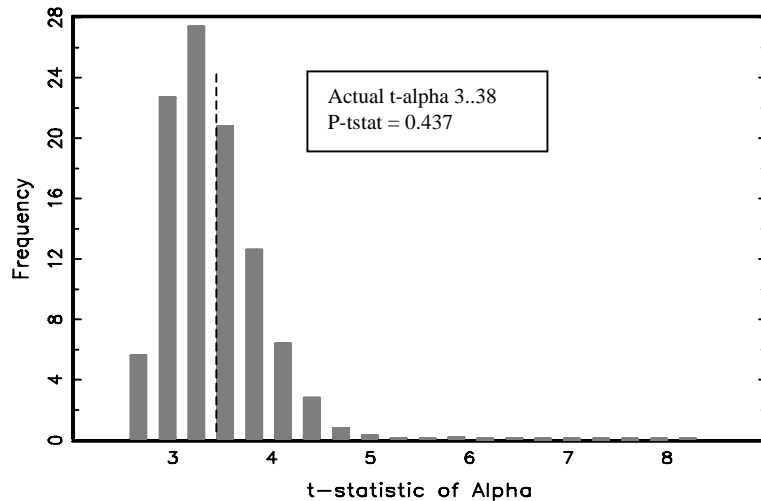
# Methodology

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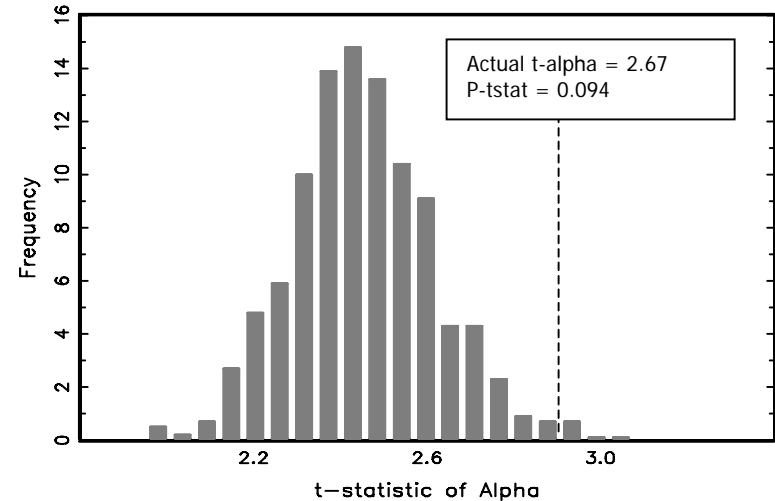
- We use the t-stat of alpha as the performance measure to (i) scale by precision and (ii) get more reliable estimates of tail performance
- Bootstrap p value:
  - Best funds: proportion of bootstrap t-alphas  $>$  actual t-alpha at each point/percentile
  - Worst funds: proportion of bootstrap t-alphas  $<$  actual t-alpha at each point/percentile
- Impose min 36 observations restriction,  $N = 675$ .
  - Shorter-lived funds  $\Rightarrow$  high  $\text{Var}(\alpha) \Rightarrow$  these funds may disproportionately occupy the tails of both bootstrap and actual distributions
  - We check if results are robust due to look-ahead bias

# Bootstrap Results : Best Funds – t-alpha

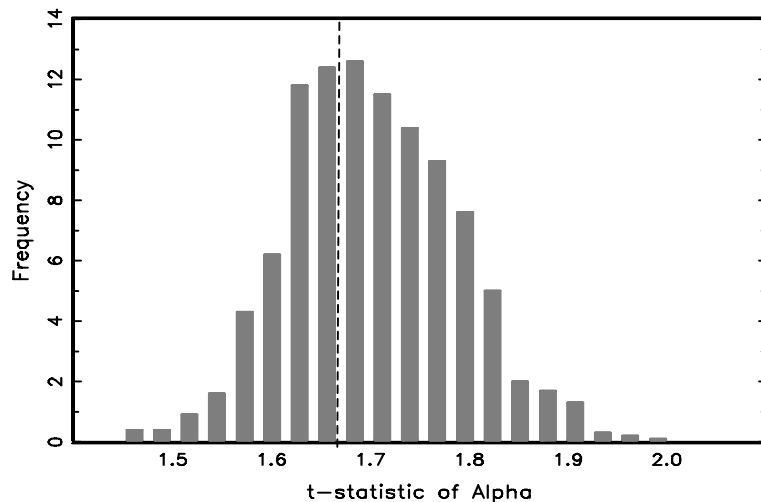
Bootstrapped t-statistics of Alpha: BEST Fund



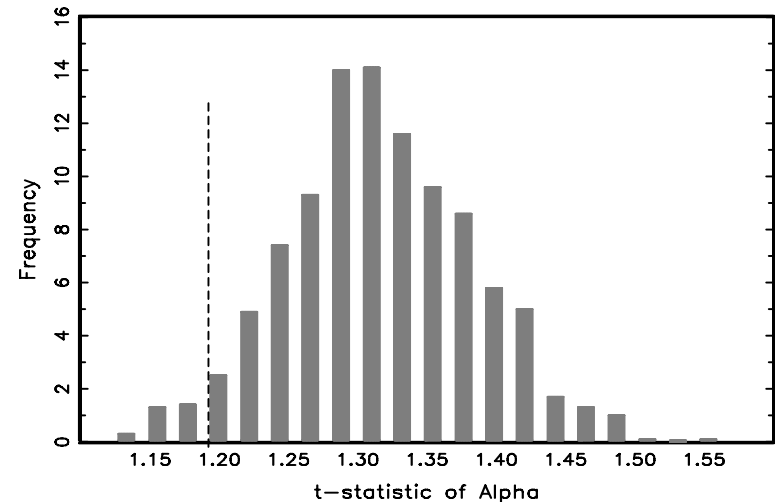
Bootstrapped t-statistics of Alpha: 99th Percentile Fund



Bootstrapped t-statistics of Alpha: 95th Percentile Fund

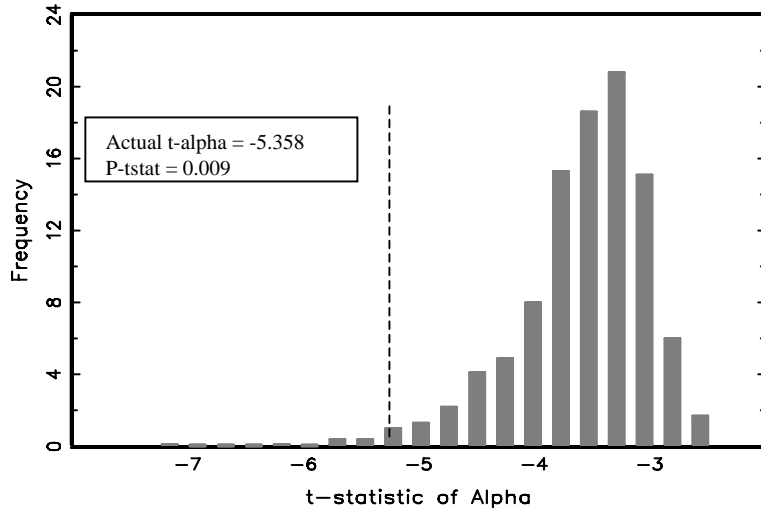


Bootstrapped t-statistics of Alpha: 90th Percentile Fund

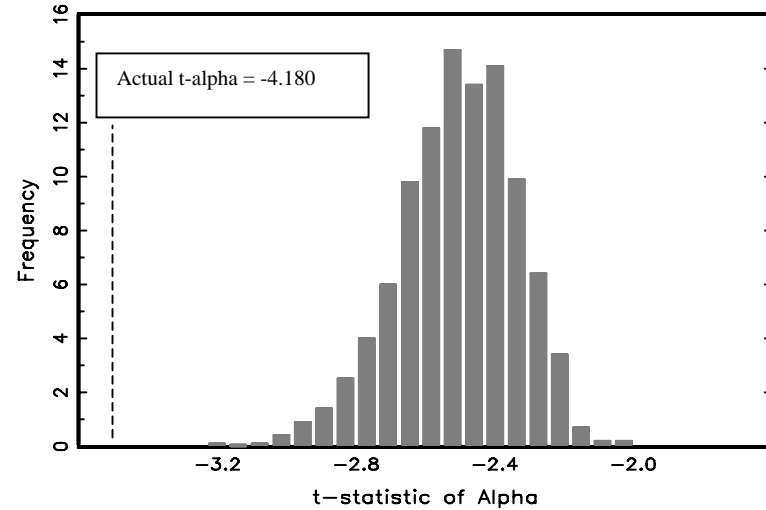


# Bootstrapped Results : Worst Funds (t-alpha)

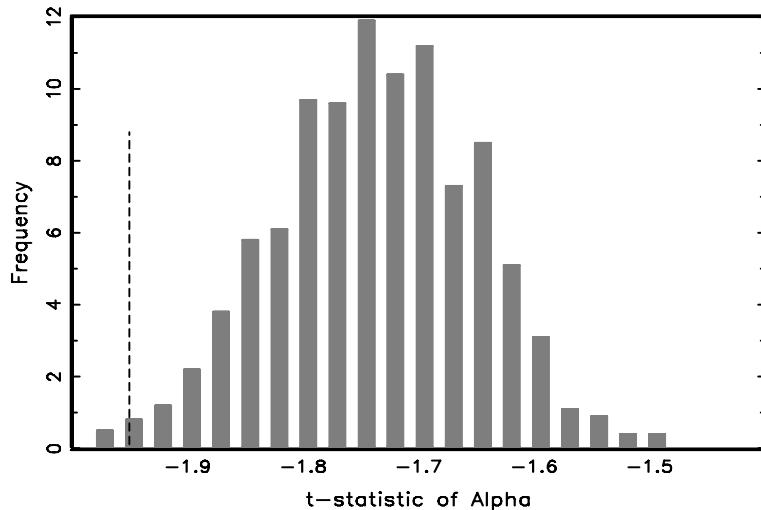
Bootstrapped t-statistics of Alpha: WORST Fund



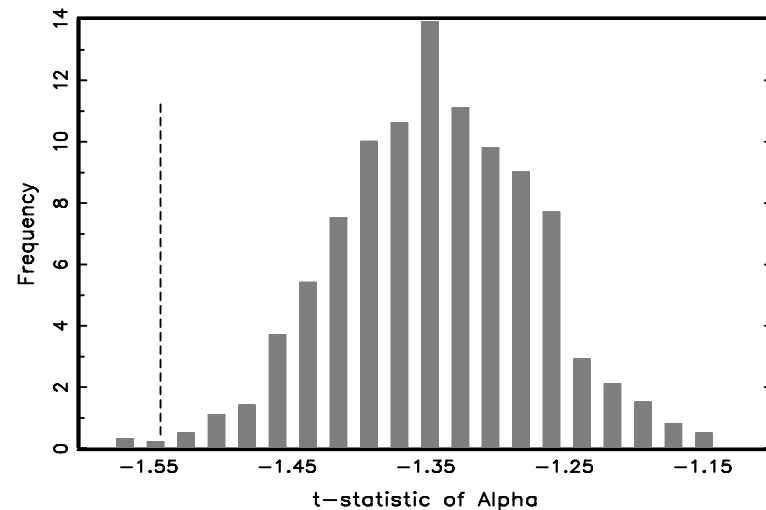
Bootstrapped t-statistics of Alpha: 1st Percentile Fund



Bootstrapped t-statistics of Alpha: 5th Percentile Fund



Bootstrapped t-statistics of Alpha: 10th Percentile Fund



# Bootstrap Statistics: p values of t-stats, BEST Funds

$$R_{i,t+1} = \alpha_i + \beta_1(R_{m,t+1}) + \beta_2(\text{SMB})_{t+1} + \beta_3(\text{HML})_{t+1} + U_{t+1}$$

| Ranked Fund | Ranked Alpha | Ranked t-stats | Significant | p-value t-stats | Stock Picking |
|-------------|--------------|----------------|-------------|-----------------|---------------|
| 1           | 2.235        | 3.389          | Sign.       | 0.437           | 'luck'        |
| 3           | 0.757        | 2.991          | Sign.       | 0.232           | 'luck'        |
| 5           | 0.716        | 2.777          | Sign.       | 0.157           | 'luck'        |
| 10          | 0.617        | 2.545          | Sign.       | 0.038           | 'skill'       |
| 12          | 0.593        | 2.501          | Sign.       | 0.020           | 'skill'       |
| 15          | 0.543        | 2.282          | Sign.       | 0.070           | 'luck'        |

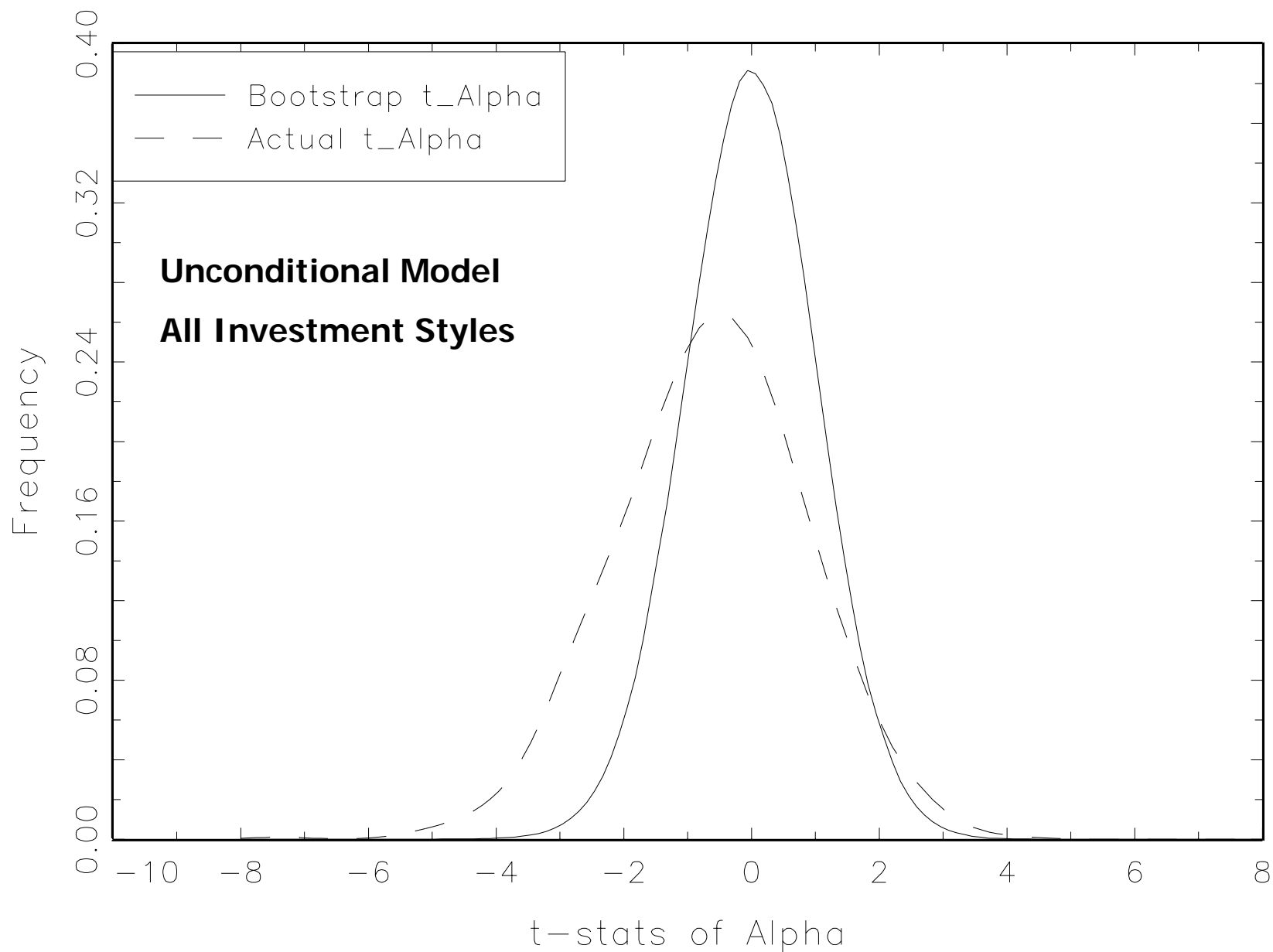
- T-stat<sub>max</sub> = 3.389 (significant), p value = 0.437 (insignificant). This contradiction is due to the highly non-normal idiosyncratic risk among top funds
- We cannot state that a fund is lucky but we cannot reject this hypothesis. We can state that a fund is skillful

# Bootstrap Statistics: p values of t-stats, WORST Funds

$$R_{i,t+1} = \alpha_i + \beta_1 (R_{m,t+1}) + \beta_2 (SMB)_{t+1} + \beta_3 (HML)_{t+1} + U_{t+1}$$

| Ranked Fund | Ranked Alpha | Ranked t-stats | Significant | p-value t-stats | Stock Picking |
|-------------|--------------|----------------|-------------|-----------------|---------------|
| Min         | -0.901       | -5.358         | Sign.       | 0.009           | Truly Bad     |
| 5. min      | -0.661       | -4.278         | Sign.       | 0.000           | Truly Bad     |
| Min. 5%     | -0.427       | -3.045         | Sign.       | 0.000           | Truly Bad     |
| Min 10%     | -0.350       | -2.509         | Sign.       | 0.000           | Truly Bad     |
| Min 40%     | -0.122       | -0.873         | Not Sign.   | 0.000           | Truly Bad     |

# Kernel Density Estimates of Actual and Bootstrap t-stats of Alpha





# Performance and Investment Styles

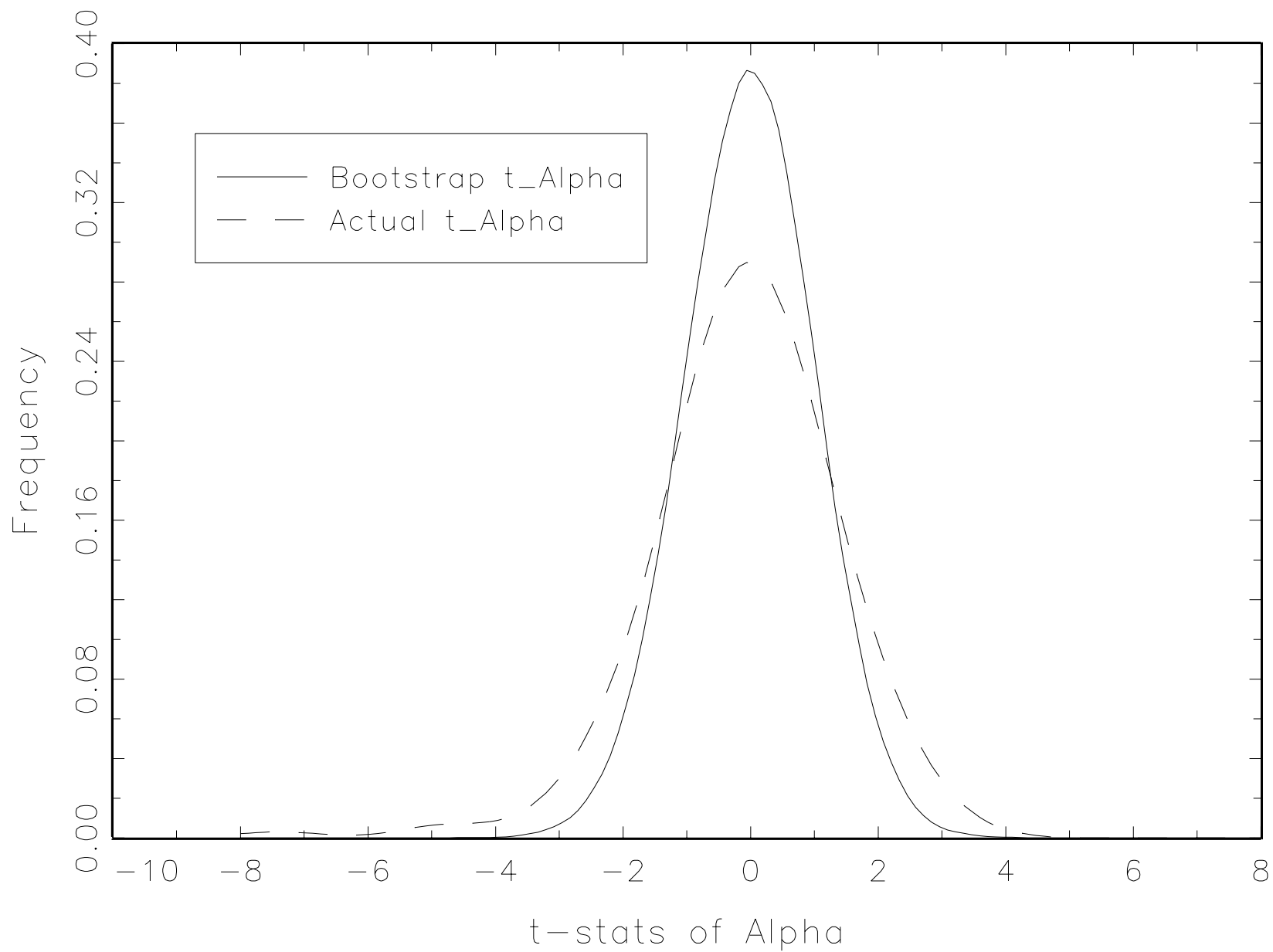
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- Does stock picking ability vary with investment objective:
  - Self-declared objectives (monitored by IMA)
  - Income, General Equity, Small Co. stocks
  - In U.S., some evidence growth funds outperform
  - Is the market for small stocks less efficient ?
- Procedure controls for investment style risk characteristics which may not be captured by performance model

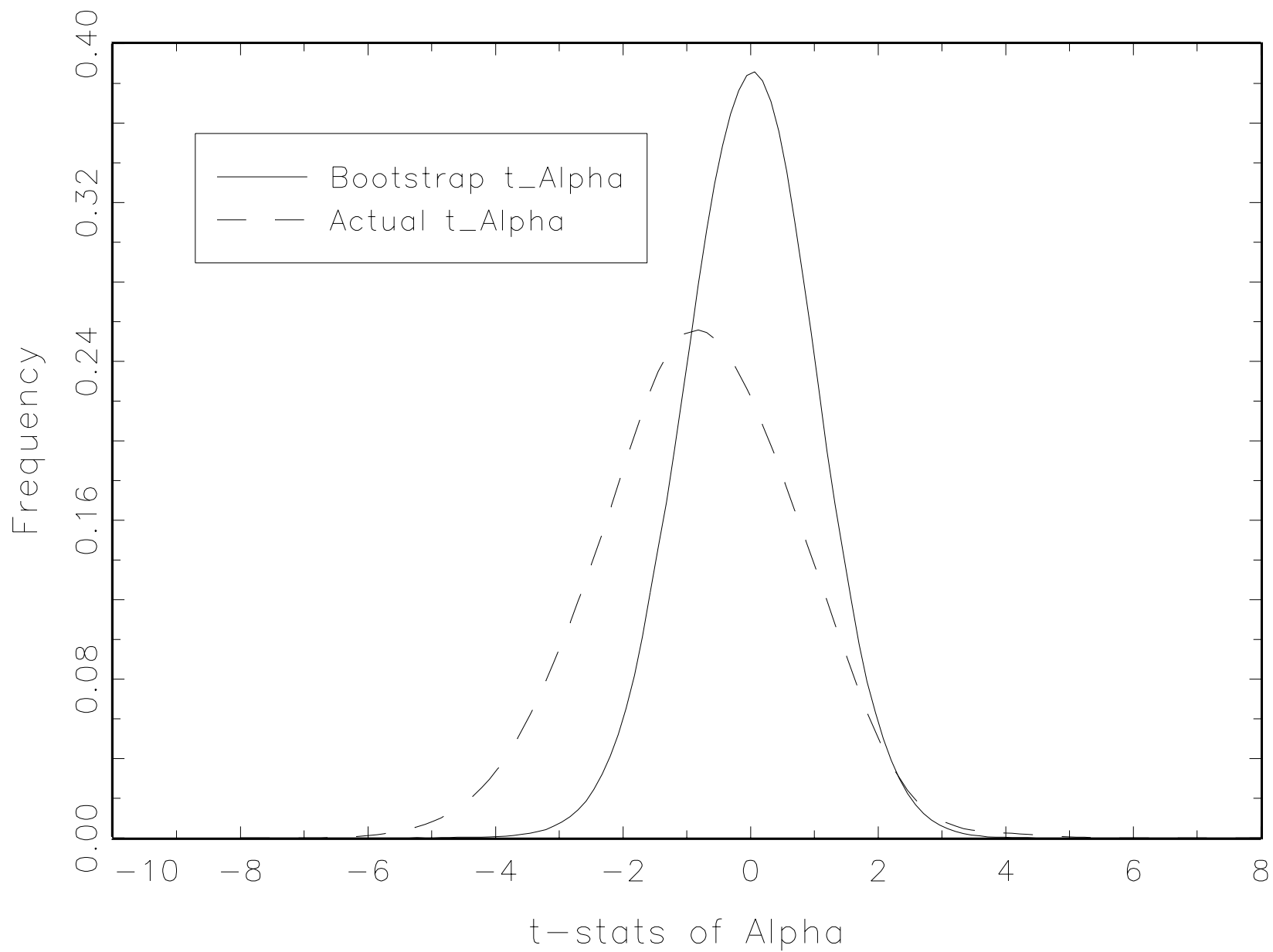
# Performance and Investment Style

|                          | Min   | 5 min  | min<br>5% | max<br>20% | max<br>10% | 10max | 7 max | 5 max | 3 max | 2 max | Max   |
|--------------------------|-------|--------|-----------|------------|------------|-------|-------|-------|-------|-------|-------|
| <b>Equity Income</b>     |       |        |           |            |            |       |       |       |       |       |       |
| T-alpha                  | -2.95 | -2.166 | -1.863    | 0.977      | 1.667      | 1.740 | 2.245 | 2.50  | 2.545 | 2.634 | 2.777 |
| Alpha                    | -0.33 | -0.204 | -0.314    | 0.470      | 0.184      | 0.275 | 0.229 | 0.302 | 0.431 | 0.279 | 0.478 |
| P-tstat                  | 0.33  | 0.165  | 0.179     | 0.171      | 0.007      | 0.107 | 0.008 | 0.005 | 0.067 | 0.181 | 0.415 |
| <b>UK All Companies</b>  |       |        |           |            |            |       |       |       |       |       |       |
| T-alpha                  | -5.36 | -4.190 | -3.118    | 0.509      | 1.045      | 2.023 | 2.282 | 2.672 | 2.776 | 2.965 | 3.389 |
| Alpha                    | -0.26 | -0.355 | -0.226    | 0.063      | 0.414      | 0.447 | 0.386 | 0.543 | 0.507 | 0.479 | 0.412 |
| P-tstat                  | 0.01  | 0.001  | 0.001     | 1.00       | 1.00       | 0.643 | 0.422 | 0.083 | 0.285 | 0.296 | 0.301 |
| <b>Smaller Companies</b> |       |        |           |            |            |       |       |       |       |       |       |
| T-alpha                  | -4.95 | -3.117 | -3.095    | 0.397      | 1.286      | 1.356 | 1.610 | 1.742 | 2.226 | 2.991 | 3.365 |
| Alpha                    | -0.35 | -0.360 | -0.479    | 0.092      | 0.253      | 0.472 | 0.318 | 0.716 | 2.235 | 0.686 | 1.447 |
| P-tstat                  | 0.00  | 0.001  | 0.001     | 1.00       | 0.647      | 0.624 | 0.490 | 0.579 | 0.256 | 0.040 | 0.096 |

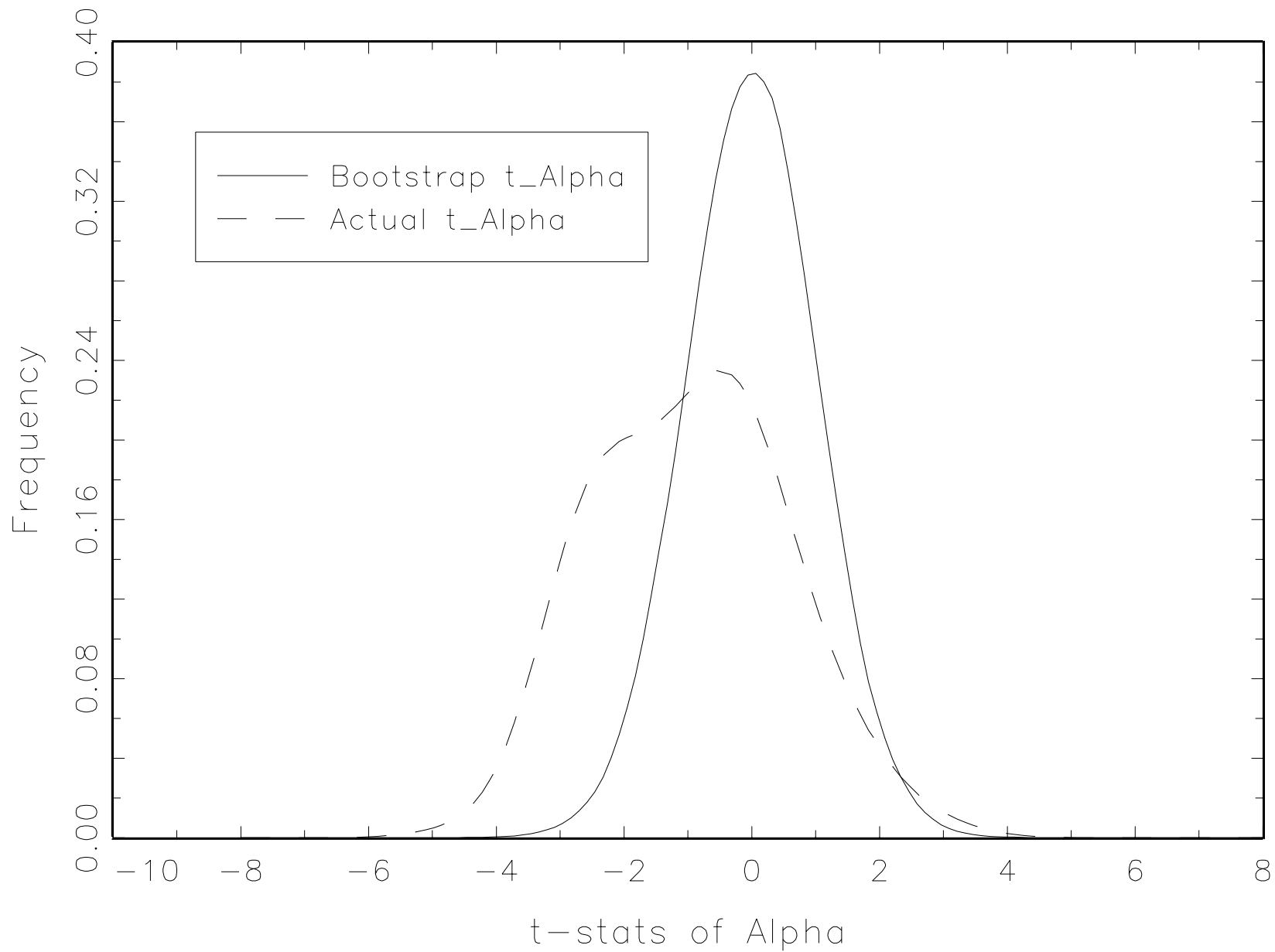
# Kernel Density Estimates: Income Funds



# Kernel Density Estimates: General Equity Funds



# Kernel Density Estimates: Small Stock Funds





# Performance and Fund Location

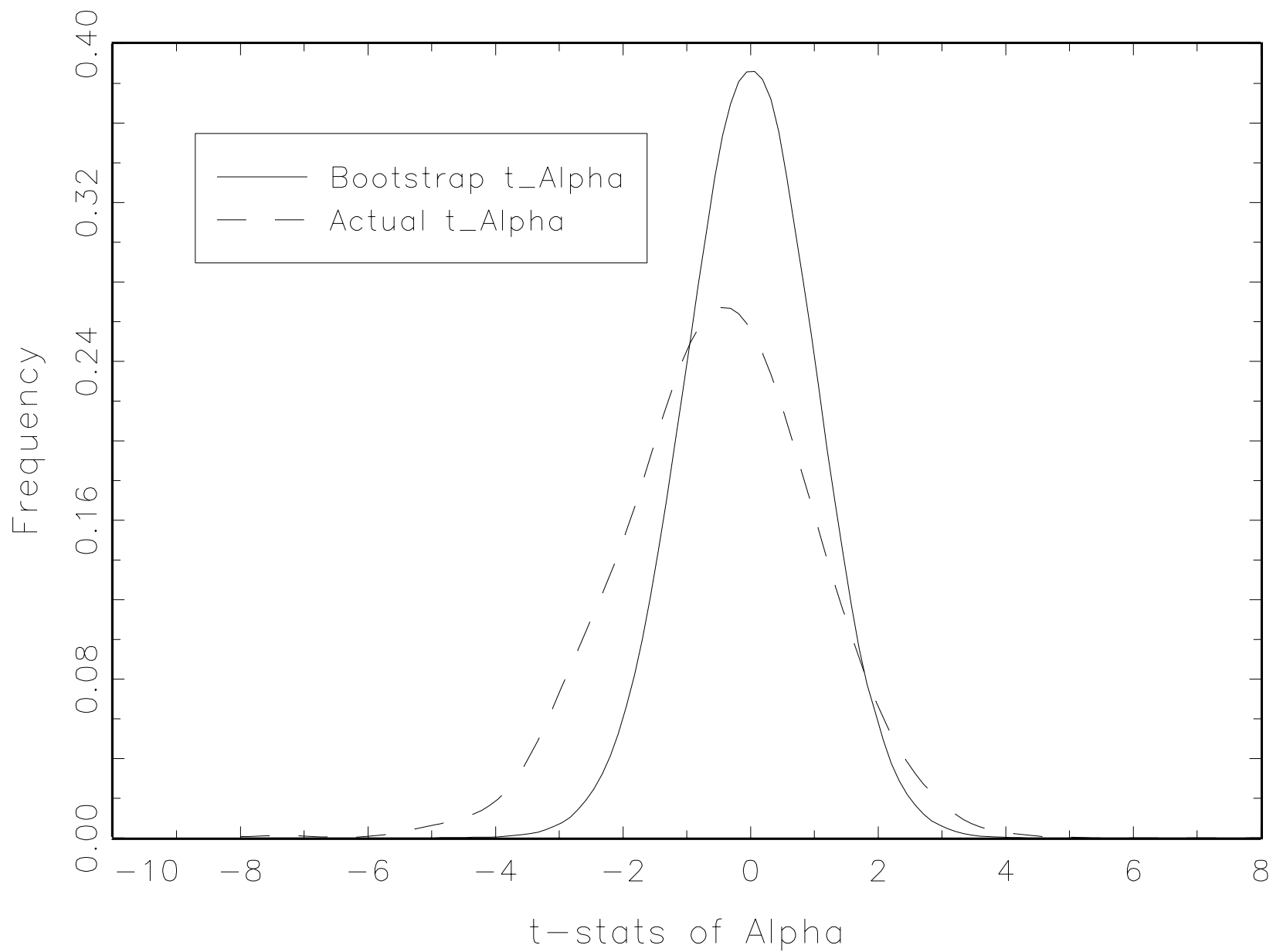
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- All funds are UK equity funds
- Onshore UK: 662 funds
- Offshore: 180 funds
  - Dublin, Luxembourg, Channel Islands, Denmark, Other European locations
- Informational Asymmetry ?
- Differences in Skill ?
- Evidence of true outperformance among Onshore funds
- Not for Offshore funds

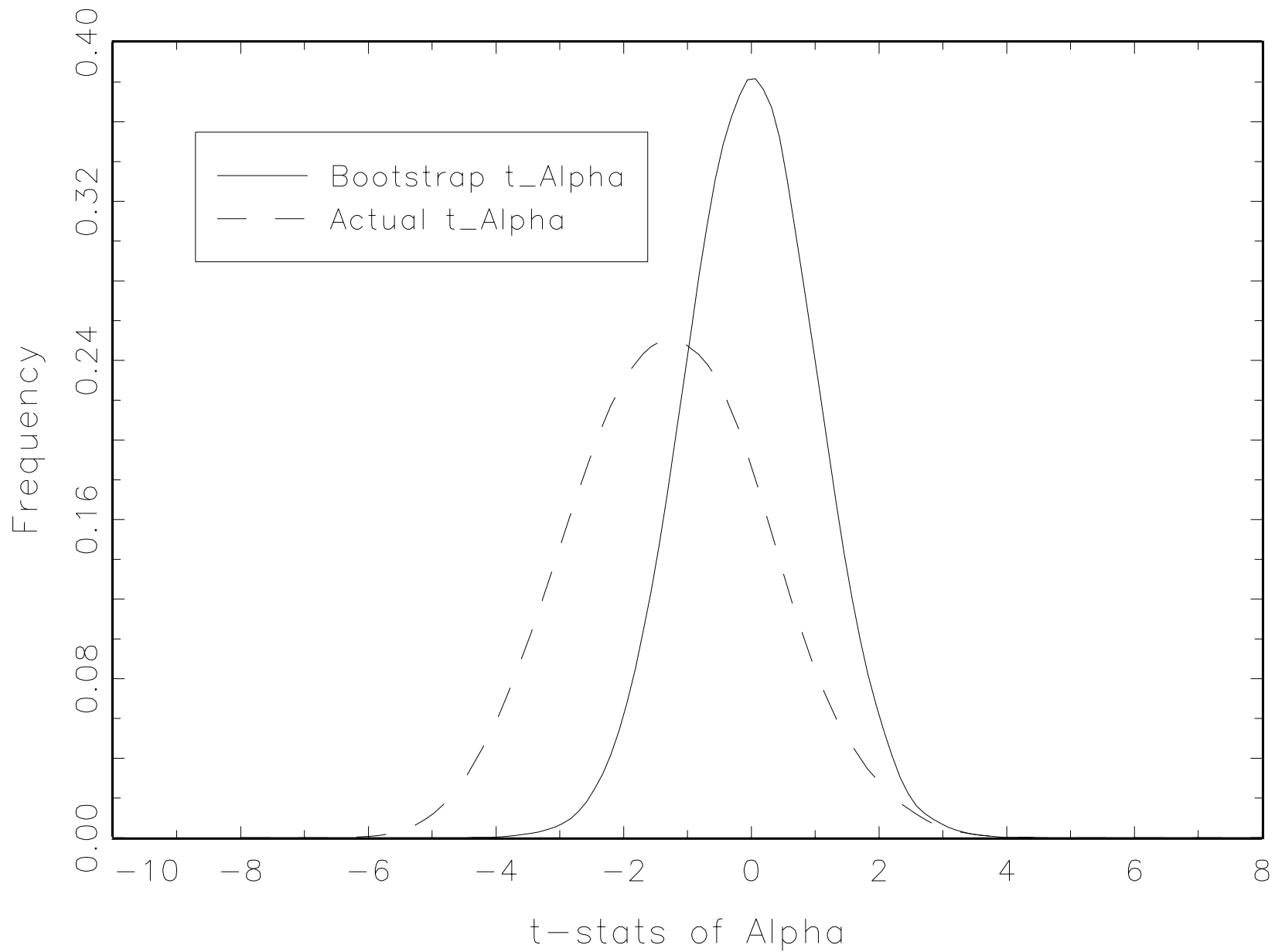
# Performance and Fund Location

|                         | Min   | 5 min  | min<br>5% | max<br>20% | max<br>10% | 20max | 10max | 5 max | 3 max | 2 max | Max   |
|-------------------------|-------|--------|-----------|------------|------------|-------|-------|-------|-------|-------|-------|
| <b>Onshore UK Funds</b> |       |        |           |            |            |       |       |       |       |       |       |
| T-alpha                 | -5.36 | -4.119 | -2.915    | 0.755      | 1.287      | 2.023 | 2.545 | 2.777 | 2.991 | 3.365 | 3.389 |
| Alpha                   | -0.26 | -0.321 | -0.510    | 0.158      | 0.130      | 0.447 | 0.431 | 0.478 | 0.686 | 1.447 | 0.412 |
| P-tstat                 | 0.01  | 0.001  | 0.001     | 0.970      | 0.615      | 0.057 | 0.006 | 0.073 | 0.107 | 0.063 | 0.306 |
| <b>Offshore Funds</b>   |       |        |           |            |            |       |       |       |       |       |       |
| T-alpha                 | -4.28 | -3.751 | -3.521    | 0.008      | 0.489      | 0.067 | 0.881 | 1.101 | 1.390 | 1.450 | 1.948 |
| Alpha                   | -0.40 | -0.414 | -0.310    | 0.004      | 0.075      | 0.006 | 0.355 | 0.588 | 0.284 | 0.593 | 0.487 |
| P-tstat                 | 0.01  | 0.001  | 0.001     | 1.000      | 1.000      | 1.000 | 1.000 | 1.000 | 0.998 | 1.000 | 0.985 |

# Kernel Density Estimates: Onshore Funds



# Kernel Density Estimates: Offshore Funds





# Survivorship Bias and Fund Histories

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- Type 1. Survivor bias
  - Analysis includes nonsurviving funds 216 (25% of sample)
- Type 2. Look-ahead bias
  - A restriction of a minimum of 36 observations is imposed
  - This improves the precision of alpha (and factor loadings) estimates
  - Shorter-lived funds => high  $\text{Var}(\alpha)$  => these funds may disproportionately occupy the tails of both bootstrap and actual distributions
  - Using bootstrap p values of t-stats mitigates.
  - However, the restriction may introduce look-ahead bias
  - We compare performance with  $T_i \geq 36$  imposed
  - Alternative minimum fund histories: 18, 36, 60, 120 obs.
  - Survivor/Nonsurvivor comparison over last 24 months



# Sensitivity Analysis & Bootstrap Extensions

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- Serial correlation and block bootstrapping
  - Residual re-sampling and the *iid* assumption
  - Residual serial correlation may incorporate valuable information as to 'true' sampling mechanism.
  - Re-sampling in blocks more closely mimics underlying return generating process.
  - Cross-sectional bootstrap procedure
- Newey-West heteroscedasticity and autocorrelation adjustments
- Alternative bootstrap procedures
  - Residual-only resampling
  - Factor-residual independent resampling
  - Factor-residual pairwise resampling (heteroscedasticity)



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End of Presentation